Homework #2

Due Monday, Feb 14, 2023, 11:59pm

Problem 2.1.

- a) Read in the 2 column data from the file 'bfit.csv' into an np.array()
- b) Print a list of the matrix, and plot the points as dots in magenta color. The x-axis is the first column, the y-axis is the second column.
- c) Calculate the bounding box, and plot a red rectangle around it
- d) Draw the diagonal from (xmin,ymin)-(xmax,ymax) in blue
- e) Overplot the points below the diagonal in green
- f) Calculate the center of mass of the points in the two halves separated by the diagonal. Plot these values shown with an asterisk on the same figure.

Problem 2.2.

- a) Create a uniform array x with 101 elements between 0 and 2*pi
- b) Create an array containing y = sin(3*x)
- c) Create a plot y vs x
- d) Create another array, z = y*y
- e) Plot z vs x
- f) Calculate the average of both y and z over this interval
- g) How do the results of (f) change if we use 10000 points?

Problem 2.3.

- a) Create a 21x21 grid of x and y values over a square [-1,1]x[-1,1]
- b) Write a function that is a Gaussian,

fgauss
$$(x, y, s) = \frac{1}{\sqrt{2\pi s^2}} \exp\left(-\frac{x^2 + y^2}{2s^2}\right)$$

c) Create a contour plot of z as a function of x,y for the values of s=1,2,3

Problem 2.4.

Consider the data in the files a100.csv, b100.csv, c100.csv and d100.csv.

a. Determine the underlying probability distributions (and its parameters) of each data set, by creating a histogram and over-plotting with the most similar probability distribution, until the agreement is acceptable. Create a label with the name of the distribution, and its parameter values on the plot. Do not use a fitting function but determine the parameters by changing them manually until there is a good visual match. The goal of this exercise is to develop an intuition on how the shapes of the different distributions change as a function of the parameters.

b. Create a new series from each data set through the formula

$$y_p = \sum_{i=0}^{K-1} x_{p+i}$$

i.e. each new number is the sum of *K* adjacent elements of the original series (so called moving average). Determine the probability distribution and its parameter for each sequence for K=5, 20 and 80. Calculate the mean and variance of the original distributions and compare to the derived (summed) series.